## References

Asano, H., Abe, Y. \& Hirabayashi, M. (1976). J. Phys. Soc. Jpn, 41, 974-976.
Asano, H. \& Hirabayashi, M. (1979). Z. Phys. Chem. (Frankfurt am Main), 114, 1-19.
Coppens, P., Guru Row, T. N., Leung, P., Stevens, E. D., Becker, P. J. \& Yang, Y. W. (1979). Acta Cryst. A35, 63-72.
Coppens, P. \& Hamilton, W. C. (1970). Acta Cryst. A26, 71-83.
International Tables for X-ray Crystallography (1959). Vol. II. Birmingham: Kynoch Press. (Present distributor D. Reidel, Dordrecht.)
International Tables for X-ray Crystallography (1969). Vol. I, 3rd ed. Birmingham: Kynoch Press.
International Tables for X-ray Crystallography (1974). Vol IV. Birmingham: Kynoch Press. (Present distributor D. Reidel, Dordrecht.)

Kajitani, T. \& Hirabayashi, M. (1985a). Z. Phys. Chem. (Frankfurt am Main), 145, 281-296.
Kajitani, T. \& Hirabayashi, M. (1985b). Private communication.
Koike, S. \& Suzuki, T. (1981). Acta Metall. 29, 553-565.
Moss, S. C. (1983). Electronic Structure and Properties of Hydrogen in Metals, edited by P. Jena \& C. B. Satterthwaite, pp. 153-163. New York: Plenum.
Noda, Y., Kajitani, T., Hirabayashi, M. \& Sato, S. (1985). Acta Cryst. C41, 1566-1571.
Okada, I., Asano, H. \& Hirabayashi, M. (1980). Trans. Jpn Inst. Met. Suppl. 21, 89-92. Hydrogen in Metals. Proc. Minakami, Japan.
Takano, S. \& Suzuki, T. (1974). Acta Metall. 22, 265-274.
Wanagel, J., Sass, S. L. \& Batterman, B. W. (1972). Phys. Status Solidi A, 10, 49-57.

# Normal Coordinate Analysis of Metal-Metal Quadruple Bonds Using a More Complete Force Field 

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#### Abstract

Normal coordinate analyses have been performed for $\mathrm{Mo}_{2}\left(\mathrm{O}_{2} \mathrm{CCH}_{3}\right)_{4}, \mathrm{Mo}_{2} \mathrm{Cl}_{8}^{4-}, \mathrm{Re}_{2}\left(\mathrm{O}_{2} \mathrm{CCH}_{3}\right)_{4} \mathrm{Cl}_{2}$ and $\mathrm{Re}_{2} \mathrm{Cl}_{8}^{2-}$ by treating each compound as an isolated molecule with $4 / \mathrm{mmm}\left(D_{4 h}\right)$ symmetry and also using the positions found in their respective crystal structures. In all cases the molecules were modelled as flexible structures with the acetate methyl groups taken as point masses. Calculated and experimental frequencies are reported along with valence bond and angle force constants. The normal modes for the $4 / \mathrm{mmm}$ models are shown and discussed for the bands observed in the experimental IR and Raman spectra of the Mo compounds. As a consequence of considering the bridging ring systems and partial Coulombic charges in the calculations for the isolated molecules and ions, values of $2 \cdot 0,2 \cdot 0,1 \cdot 1$ and $1.9 \mathrm{~N} \mathrm{~m}^{-1}$, respectively, are obtained for the $M \equiv M$ force constants. When the intermolecular interactions in the solids are considered, somewhat lower values, $1 \cdot 8,1 \cdot 7,1.0$ and $1.9 \mathrm{~N} \mathrm{~m}^{-1}$, respectively, are obtained.


## Introduction

Normal coordinate analyses have been performed for polycyclic inorganic compounds but little has been

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done with systems having both multiple metal-metal bonds and bridging ring systems. An early analysis was performed on $\mathrm{Cr}_{2}\left(\mathrm{O}_{2} \mathrm{CCH}_{3}\right)_{4} \cdot 2 \mathrm{H}_{2} \mathrm{O}$ by Costa, Pauluzzi \& Puxeddu (1957) to determine the force constants in the acetate groups but only the $\mathrm{C}-\mathrm{C}$ and $\mathrm{C}-\mathrm{O}$ stretching force constants were considered; the metal-metal bond and metal-ligand interactions were ignored. Vibrational analyses for compounds with bridging acetates have recently been published, but no normal coordinate calculations were carried out and the compounds did not have metal-metal bonds (Johnson, Cannon \& Powell, 1981, 1982). The vibrational spectrum of $\mathrm{Cu}_{2}\left(\mathrm{O}_{2} \mathrm{CCH}_{3}\right)_{4} \cdot 2 \mathrm{H}_{2} \mathrm{O}$ has been examined, but again no normal coordinate analysis was done and the $\mathrm{Cu}-\mathrm{Cu}$ interaction is considered to be nonbonding (Shriver, Mathey \& Greig, 1982). The compounds to be examined here were previously subjected to normal coordinate analysis (Bratton, Cotton, Debeau \& Walton, 1971; Ketteringham, Oldham \& Peacock, 1976), but only the $M_{2} X_{8}$ portion of the molecules was used and the effects of the bridging rings and residual charges were ignored. We have chosen to do a more complete vibrational analysis of these compounds to explore the effects of the acetate bridges and residual charges on their molecular vibrations with a view toward obtaining a more accurate picture of the multiple metal-metal bond. Although we were able to obtain all the spectra needed for this study from the literature, there were conflicting Raman spectra for
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$\mathrm{Mo}_{2}\left(\mathrm{O}_{2} \mathrm{CCH}_{3}\right)_{4}$ (Bratton et al., 1971; San Filippo \& Sniadoch, 1973). Thus, we remeasured both the IR and Raman spectra of this compound.

## Experimental

The sample of $\mathrm{Mo}_{2}\left(\mathrm{O}_{2} \mathrm{CCH}_{3}\right)_{4}$ was prepared by previously published methods (Cotton \& Brignole, 1972). As this compound is somewhat air and moisture sensitive all manipulations were carried out in a drybox. IR spectra were obtained from KBr pellets ( $3000-600 \mathrm{~cm}^{-1}$ ) and Nujol mulls between polyethylene plates $\left(600-300 \mathrm{~cm}^{-1}\right)$ on a Nicolet MX-1 Fourier-transform infrared spectrometer. The KBr and Nujol were carefully dried before use. Raman spectra were obtained from powdered samples enclosed in sealed glass tubes. The spinning sample technique was used to prevent burning of the samples by the laser beam. The Raman instrument is a Spex model 1402 which has been extensively modified. The $6471 \AA$ Iine of a Spectra Physics 165 krypton laser was used as the excitation source to minimize sample absorption.

## Calculations

All calculations were performed on an IBM 3081 computer using the program WMIN (Busing, 1980). Although the principal purpose of WMIN is to model structures by using potential-energy functions, it will do normal coordinate calculations based on structural data, bond and angle force constants, Coulombic charges and nonbonded interatomic interaction potentials (Gilbert, 1968). The more commonly used normal coordinate analysis programs (e.g., Schachtschneider, 1965), express all the interaction effects as force constants via a Urey-Bradley formalism even though most interactions are nonbonding. Moreover, the force constant for each unique interaction is treated separately even though the same interatomic potential function could be applied to many different interatomic interactions. As a result, most analyses using this type of calculation have many of the interaction force constants arbitrarily set to zero in order to reduce the parameterization to match the number of available spectral lines. Because it uses a more generalized set of interatomic potentials, WMIN can describe a vibrational model with fewer parameters, all of which can be related more closely to physical quantities such as Coulombic charge and nonbonded radii. However, it is unable to refine these coefficients by matching the calculated vibrational energies to the observed IR and Raman spectra, thus we were required to use trial and error procedures to obtain our best estimates of the force constants and other coefficients.
For this study two vibrational models were examined for each compound. One model consisted
of an isolated molecule with the idealized point group $D_{4 h}$ and Cartesian atomic coordinates obtained in each case by averaging the molecular geometries obtained from the crystal structures of $\mathrm{Mo}_{2}\left(\mathrm{O}_{2} \mathrm{CCH}_{3}\right)_{4}$ (Cotton, Mester \& Webb, 1974), $\mathrm{Re}_{2}\left(\mathrm{O}_{2} \mathrm{CCH}_{3}\right)_{4} \mathrm{Cl}_{2}$ (Kosmin, Surazhskaya, Larina, Kotelnikova \& Misailova, 1980), $\mathrm{K}_{4} \mathrm{Mo}_{2} \mathrm{Cl}_{8} \cdot 2 \mathrm{H}_{2} \mathrm{O}$ (Brencic \& Cotton, 1969), and [( $n-\mathrm{Bu})_{4} \mathrm{~N}_{2}\left[\mathrm{Re}_{2} \mathrm{Cl}_{8}\right]$ (Cotton, Frenz, Stults \& Webb, 1976). The other model used the real crystallographic symmetry for each solid compound. For the first two compounds the methyl groups were considered to be point masses ( $M=15 \cdot 01$ a.m.u.) to maintain $4 / \mathrm{mmm}$ symmetry for the isolated molecules and because the hydrogen atoms were not located in their crystal structures. Thus the calculated vibrational modes do not include hydrogen motion.
The potential-energy functions for these calculations used bond and angle force constants ( $K$ ) for the bonded interatomic interactions, Coulombic charges $\left(q_{i}\right)$ where necessary, and nonbonded interaction coefficients ( $a_{i}, b_{i}$ and $p_{i}$ ). The functions were of the form

$$
\begin{aligned}
V= & \sum \frac{K}{2}\left(d-d_{0}\right)^{2}+\sum \frac{K}{2}\left(\theta-\theta_{0}\right)^{2}+\frac{1}{2} \sum q_{i} q_{j} / r_{i j} \\
& +\sum f\left(b_{i}+b_{j}\right) \exp \left[\left(a_{i}+a_{j}-r_{i j}\right) /\left(b_{i}+b_{j}\right)\right] \\
& -\frac{1}{2} \sum p_{i} p_{j} / r_{i j}^{6}
\end{aligned}
$$

where $f$ scales the repulsion term to give the appropriate potential-energy units. For the isolated molecule the summations were performed over the entire molecule and for the crystal an accelerated convergence Ewald sum over the lattice was performed. The equilibrium distances, $d_{0}$, and angles, $\theta_{0}$, were those found in the crystal structures. The bond and angle force constants (Tables 1 and 2 ) involving the metal atoms were obtained by trial and error fitting of the calculated vibrational energies to the observed IR and Raman spectra. They will be discussed below. Initial values for other bond and angle force constants (Table 1) were set at reasonable values and subsequently adjusted by trial and error; torsional force constants were ignored. In the case of the two $M_{2} \mathrm{Cl}_{8}^{n-}$ anions, the excess negative charge was distributed equally among the eight Cl atoms, and the counter ions for the crystal calculations were placed as point charges. The nonbonded interaction coefficients (Table 3) are nonbonded radii $\left(a_{i}\right)$, repulsion coefficients ( $b_{\mathrm{i}}$ ) and softness coefficients ( $p_{i}$ ). The nonbonded radii for $\mathrm{C}, \mathrm{O}$ and methyl are from Bondi (1964) and Pauling (1960), and those for Mo and Re are from Slater (1964). The repulsion coefficients and the nonbonded radius of Cl are those of Busing (1980) with the values for the metals estimated from other known values. The softness coefficients for C and O were taken from Busing (1980) and the others were

Table 1. Force constants for the acetates $\left(\mathrm{N} \mathrm{m}^{-1}\right.$ or $\mathrm{J} \mathrm{rad}{ }^{-2} \times 10^{18}$ )

| Linkage | $\mathrm{Mo}_{2}\left(\mathrm{O}_{2} \mathrm{CCH}_{3}\right)_{4}$ |  | $\mathrm{Re}_{2}\left(\mathrm{O}_{2} \mathrm{CCH}_{3}\right)_{4} \mathrm{Cl}_{2}$ |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Crystal | Molecule | Crystal | Molecule |
| K(MM) | 1.8 | $2 \cdot 0$ | 1.0 | $1 \cdot 1$ |
| $K(M O)$ | 1.6 | 1.7 | $2 \cdot 2$ | $2 \cdot 2$ |
| $K(0 C)$ | 4.9 | 4.9 | 4.9 | 4.9 |
| $K(\mathrm{CMe})$ | $1 \cdot 25$ | $1 \cdot 25$ | 1.25 | $1 \cdot 25$ |
| $\boldsymbol{K}(\mathbf{M C l})$ | - | - | 0.45 | $0 \cdot 45$ |
| K(OCO) | $3 \cdot 0$ | 2.9 | 1.7 | 1.7 |
| K (OCMe) | 0.46 | 0.46 | $0 \cdot 46$ | $0 \cdot 46$ |
| K (MOC) | $2 \cdot 5$ | $2 \cdot 5$ | 3.0 | $3 \cdot 0$ |
| $K(O M M)$ | 4.9 | $5 \cdot 1$ | 0.94 | 0.94 |
| $K(O M O){ }_{\text {cis }}$ | 13.0 | $12 \cdot 9$ | 9.0 | $9 \cdot 0$ |
| $\mathrm{K}(\mathrm{OMO})_{\text {trans }}$ | $2 \cdot 6$ | $2 \cdot 3$ | 3.9 | 3.9 |
| $K(O M C l)$ | - | - | $3 \cdot 5$ | $3 \cdot 5$ |
| $K(M M C l)$ | - | - | $7 \cdot 6$ | $7 \cdot 6$ |

Table 2. Force constants for the chlorides $\left(\mathrm{N} \mathrm{m}^{-1}\right.$ or $\mathrm{J} \mathrm{rad}^{-2} \times 10^{18}$ )

|  | $\mathrm{Mo}_{2} \mathrm{Cl}_{8}^{4-}$ |  | $\mathrm{Re}_{2} \mathrm{Cl}_{8}^{2-}$ |  |
| :--- | :---: | :---: | :---: | :---: |
| Linkage | Crystal | Free ion | Crystal | Free ion |
| $K(M M)$ | 1.7 | 2.0 | 1.9 | 1.9 |
| $K(M \mathrm{Ml})$ | 0.73 | 0.74 | 0.92 | 0.92 |
| $K(M M C l)$ | 0.50 | 0.50 | 0.32 | 0.32 |
| $K(\mathrm{ClMCl})_{\text {cis }}$ | 2.7 | 2.7 | 4.2 | 4.0 |
| $K(C l M \mathrm{Cl})_{\text {rran }}$ | 1.14 | 1.14 | 2.4 | 2.5 |

estimated by trial and error during this work. These coefficients were used in the isolated-molecule calculations for intramolecular interactions and in the crystal calculations for both intramolecular and intermolecular interactions. For the crystal calculations the surrounding molecules were assumed to be fixed in position and hence the calculations only yield internal molecular modes. In each case a survey of possible values of the unknown force constants was made to determine the sensitivity of the calculated vibrational energies; the range of values tested covered approximately an order of magnitude about their final values. This survey included the commonly accepted values where available from Urey-Bradley calculations (Nakamoto, 1963). Then the values of the force constants were adjusted to their best values by successive calculations until a reasonable agreement between the energy of the observed IR and Raman bands and their calculated values was obtained; the average discrepancy is $\sim 8 \mathrm{~cm}^{-1}$ for the four isolated-molecule calculations. In all cases there was sufficient sensitivity in the calculated vibrational energies to estimate the force constants to $5 \mathbf{- 1 0 \%}$.

## Results and discussion

Our best estimates of the force constants for the bonds and angles in all four compounds, both for isolated molecules and for the solid crystalline structures, are given in Tables 1 and 2. Nonbonded potential coefficients used in these calculations are given in Table 3. As expected, the various values involving

Table 3. Coefficients for interatomic potential functions

|  | $a_{i}(\AA)$ | $b_{i}(\AA)$ | $p_{i}\left(\AA^{3}\right)$ |
| :--- | :---: | :---: | :---: |
| O | 1.50 | 0.14 | 20.5 |
| C | 1.70 | 0.14 | 16.1 |
| CH | 2.00 | 0.14 | 16.1 |
| Cl | 2.43 | 0.24 | 18.0 |
| Mo | 1.45 | 0.04 | 30.0 |
| $\operatorname{Re}$ | 1.45 | 0.05 | 27.0 |

Nonbonded interaction coefficients: $a_{i}$, nonbonded radii; $b_{i}$, repulsion coefficients; $p_{i}$, softness coefficients.

Table 4. Observed and calculated vibrational modes for $\mathrm{Mo}_{2}\left(\mathrm{O}_{2} \mathrm{CCH}_{3}\right)_{4}$
Obsd (cm

$1518(I)$
$1413(I)$
$948(R)$
$937(I) \ddagger$

|  | $731 / 728$ | $2 A_{g}$ |
| :--- | :--- | :--- |
|  | 727 | $A_{u}$ |
| $692(R)$ | 703 | $A_{g}$ |
| $685(R)$ | 701 | $A_{g}$ |
| $674(I)$ | $698 / 697$ | $2 A_{u}$ |
| $628(I)$ | 612 | $A_{u}$ |
| $488(R)$ | $489 / 482$ | $2 A_{g}$ |
|  | 494 | $A_{u}$ |
| $413(R) \S$ | 411 | $A_{g}$ |
| $406(R)$ | 406 | $A_{g}$ |
| $368 / 337(I)$ | $366 / 359$ | $2 A_{u}$ |
| $322 / 315(R)$ | $319 / 309$ | $2 A_{g}$ |
| $299(R)$ | $306 / 298$ | $2 A_{g}$ |


| $P \overline{1}$ calcd $\left(\mathrm{cm}^{-1}\right)$ |  |
| :--- | :--- |
| 1530 | $A_{g}$ |
| 1521 | $A_{g}$ |
| $1527 / 1519$ | $2 A_{u}$ |
| 1411 | $A_{u}$ |
| 1402 | $A_{u}$ |
| $1391 / 1387$ | $2 A_{g}$ |
| 1105 | $A_{g}$ |
| 1102 | $A_{u}$ |
| 1030 | $A_{g}$ |
| 992 | $A_{8}$ |
| $950 / 933$ | $2 A_{g}$ |
| $938 / 930$ | $2 A_{u}$ |
| $914 / 903$ | $2 A_{u}$ |
| 752 | $A_{u}$ |
| $731 / 728$ | $2 A_{g}$ |
| 727 | $A_{u}$ |
| 703 | $A_{g}$ |
| 701 | $A_{g}$ |
| $698 / 697$ | $2 A_{u}$ |
| 612 | $A_{u}$ |
| $489 / 482$ | $2 A_{g}$ |
| 494 | $A_{u}$ |
| 411 | $A_{g}$ |
| 406 | $A_{g}$ |
| $366 / 359$ | $2 A_{u}$ |
| $319 / 309$ | $2 A_{g}$ |
| $306 / 298$ | $2 A_{g}$ |


| $D_{4 h}$ calcd $\left(\mathrm{cm}^{-1}\right)$ |  |
| :--- | :--- |
| 1525 | $A_{1 g}$ |
| 1520 | $B_{1 g}$ |
| 1520 | $E_{u}$ |
| 1411 | $A_{2 u}$ |
| 1403 | $B_{2 u}$ |
| 1391 | $E_{g}$ |
| 1098 | $B_{2 g}$ |
| 1097 | $B_{1 u}$ |
| 1024 | $A_{1 g}$ |
| 985 | $B_{18}$ |
| 946 | $E_{g}$ |
| 933 | $E_{u}$ |
| 912 | $E_{u}$ |
| 752 | $A_{2 u}$ |
| 732 | $E_{g}$ |
| 729 | $B_{2 u}$ |
| 703 | $A_{1 g}$ |
| 697 | $B_{1 g}$ |
| 695 | $E_{u}$ |
| 607 | $A_{2 u}$ |
| 491 | $E_{g}$ |
| 488 | $B_{2 u}$ |
| 413 | $A_{1 g}$ |
| 406 | $A_{1 g}$ |
| 360 | $E_{u}$ |
| 307 | $E_{g}$ |
| $303 / 302$ | $B_{1 g} / A_{1 g}$ |

Mode
$1518(I)$
$1413(I)$
$\dagger$ Both IR and Raman active bands are shown and marked accordingly. $\ddagger$ This band was not observed by us; however, it was reported by Bratton, Cotton, Debeau \& Walton (1971).
$\S$ This band observed for ${ }^{92} \mathrm{Mo}_{2}\left(\mathrm{O}_{2} \mathrm{CCH}_{3}\right)_{4}$ (Shriver, Cooper, Hutchinson, Morgan \& Mathey, 1979).
bonds common to both Mo and Re molecules are usually identical while those involving the metal atoms are quite different. The calculated vibrational frequencies and Mulliken symbols for isolated molecules and crystalline solids of the four compounds are shown in Tables 4-7; the observed values are also given for comparison. Those modes involving principally torsional motion are not listed in the tables. Figs. 1 and 2 show the direction and magnitude of the atomic displacements for the vibrational modes assigned a roman numeral in Tables 4 and 6, respectively. The major axis of each atomic ellipsoid is proportional to the atomic displacement; the minor axes are of arbitrary dimensions. These drawings were made using a locally modified version of ORTEPII (Johnson, 1976). The modes assigned roman numerals in Tables 5 and 7 have similar displacements to those shown in the figures. In most cases the vibrational modes so marked for all four compounds correspond in energy to bands in the observed spectra.

Table 5. Observed and calculated vibrational modes for $\mathrm{Re}_{2}\left(\mathrm{O}_{2} \mathrm{CCH}_{3}\right)_{4} \mathrm{Cl}_{2}$

| Obsd ( $\left.\mathrm{cm}^{-1}\right)^{*}$ | $P 2 / n$ calcd ( $\mathrm{cm}^{-1}$ ) |  | $D_{4 n}$ calcd ( $\mathrm{cm}^{-1}$ ) |  | Mode |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1439 | $A_{\mu}$ | 1441 | $\mathrm{A}_{2 u}$ | II |
|  | 1432 | $A_{u}$ | 1434 | $B_{2 u}$ | - |
|  | 1408 | $2 B_{g}$ | 1408 | $E_{g}$ | - |
|  | 1396 | $\mathrm{A}_{8}{ }^{8}$ | 1393 | $A_{18}{ }_{\text {g }}$ | - |
|  | 1390 | $A_{8}^{8}$ | 1388 | $B_{18}^{18}$ | - |
| 1385(I) | 1392/1389 | $2 B_{u}$ | 1388 | $E_{u}$ | 1 |
|  | 1072 | $A_{g}$ | 1076 | $A_{18}$ | - |
|  | 1043 | $A_{8}^{8}$ | 1046 | $B_{18}$ | - |
| 965(R) | 966 | $A_{8}^{8}$ | 967 | $B_{28}$ | - |
|  | 971 | $A_{\mu}^{8}$ | 964 | $B_{14}$ | - |
| 952(I) | 953/941 | $2 B_{u}$ | 954 | $E_{u}$ | IV |
| $918(R)$ | 913/903 | $2 B_{8}$ | 911 | $E_{8}$ | 111 |
|  | 895/887 | $2 B_{u}$ | 894 | $E_{u}^{\text {g }}$ | - |
|  | 808 | $A_{4}$ | 808 | A $_{24}$ | - |
|  | 797/792 | $2{ }^{4}$ | 793 | $E_{8}$ | - |
|  | 794 | $A_{u}{ }^{8}$ | 792 | $B_{2 u}$ | - |
| $721(R)$ | 721 | $A_{8}$ | 714 | $A_{18}$ | v |
| $704(R)$ | 715 | $B_{88}^{8}$ | 711 | $B_{18}$ | VI |
| $685(\mathrm{I})$ | 716/711 | $2{ }^{8}{ }_{u}$ | 710 | $E_{u}$ | VII |
| 629(I) | 624 | $A_{u}{ }^{\prime}$ | 626 | $A_{2 u}$ | VIII |
|  | 551 | $A_{\mu}$ | 553 | $B_{24}$ | - |
|  | 509/499 | $2 B_{8}$ | 503 | $E_{8}$ | IX |
| $397(R)$ | 405/397 | $2 B_{g}$ | 403 | $E_{g}^{8}$ | XII |
| 396/390(I) | 399/394 | $2 B_{u}$ | 392 | $E_{u}$ | - |
|  | 355 | $A_{8}$ | 346 | $A_{18}$ | XIII |
| 356(I) | 364/352 | $2 B_{u}$ | 340 | $E_{4}{ }^{1}$ | XI |
|  | 345 | $A_{8}$ | 339 | $B_{18}$ | - |
| $289(R)$$220(I)$ | 289 | $A_{\mathrm{g}}^{\mathrm{g}^{\text {b }}}$ | 289 | $A_{18}$ | x |
|  | 250/240 | ${ }^{2 B}{ }_{8}$ | 227 | $E_{8}$ | - |
| 220(I) | 218 | $A_{\mu}$ | 208 | $A_{2 \mu}$ | - |

* Observed spectra from Bratton, Cotton, Debeau \& Walton (1971) and Ketteringham, Oldham \& Peacock (1976).

Table 6. Observed and calculated vibrational modes for $\mathrm{K}_{4} \mathrm{Mo}_{2} \mathrm{Cl}_{8} .2 \mathrm{H}_{2} \mathrm{O}$

| Obsd ( $\left.\mathrm{cm}^{-1}\right)^{*}$ | Pbam calcd ( $\mathrm{cm}^{-1}$ ) |  | $D_{4 h}$ calcd ( $\mathrm{cm}^{-1}$ ) |  | Mode |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 346(R) | 352 | $A_{8}$ | 359 | $A_{18}$ | 1 |
|  | 342 | $B_{18}$ | 341 | $B_{28}$ | - |
|  | 341 | $A_{u}$ | 331 | $B_{14}$ | - |
| $315(R)$ | 317/312 | $B_{38} / B_{28}$ | 314 | $E_{8}$ | II |
| $307(\mathrm{I})$ | 310/309 | $B_{3 u} / B_{2 k}$ | 306 | $E_{u}{ }^{\text {c }}$ | III |
| $277(R)$ | 303 |  | 276 | $A_{18}$ | IV |
| 275(I) | 283 | $B_{14}^{8}$ | 276 | $\mathrm{A}_{24}$ | v |
|  | 264/262 | $B_{3 u} / B_{2 u}$ | 263 | $E_{u}{ }^{\text {u }}$ | - |
|  | 262 | $A_{u}{ }^{\text {a }}$ | 255 | $A_{2 u}$ | - |
| 277/253(R) | 269/259 | $B_{28} / B_{38}$ | 252 | $E_{g}$ | VI |
|  | 227 |  | 215 | $A_{18}{ }_{18}$ | - |
|  | 214 | $A_{8}^{8}$ | 214 | $B_{18}^{18}$ | - |
| $191(\mathrm{R})$ | 193 | $A_{8}^{8}$ | 172 | $B_{18}^{18}$ | VII |
| 182(I) | 209 | $B_{1 u}^{8}$ | 174 | $B_{24}$ | VIII |
| 182/160(I) | 174/163 | $B_{2 u} / B_{3 u}$ | 168 | $E_{u}$ | IX |
|  | 111/94 | $B_{2 g} / B_{3 g}$ | 109 | $E_{8}$ |  |
| 130(I) | 109 | $B_{1 u}{ }^{28}$ | 106 | $\mathrm{B}_{24}^{8}$ | x |

* Observed spectra from Clark \& Franks (1975).

Table 7. Observed and calculated vibrational modes for $\left[(n-\mathrm{Bu})_{4} \mathrm{~N}\right]_{2}\left[\mathrm{Re}_{2} \mathrm{Cl}_{8}\right]$

| Obsd ( $\left.\mathrm{cm}^{-1}\right)^{*}$ | $P 2_{1} / \mathrm{ccalcd}\left(\mathrm{cm}^{-1}\right)$ |  | $D_{4 h}$ calcd ( $\mathrm{cm}^{-1}$ ) |  | Mode |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 431 | $A_{8}$ | 437 | $B_{B_{28}}$ | - |
|  | 423 | $\boldsymbol{A}_{\boldsymbol{u}}{ }^{\text {r }}$ | 429 | $B_{14}$ | - |
| $356(R)$ | 359 | $A_{8}$ | 369 | ${ }_{\text {A }}^{18}$ | I |
| 346/338(I) | 342/341 | ${ }^{\text {2 }}{ }_{\text {bu}}$ | 339 | $E_{u}$ | III |
| 332(I) | 307 | $A_{u}{ }^{\text {u }}$ | 320 | $\boldsymbol{A}_{2 \mu}$ | v |
| 327/310(R) | 335/334 | $2 \mathrm{~B}_{8}$ | 332 | $E_{8}$ | II |
| $295(R)$ | 308 | $A_{8}{ }^{8}$ | 318 | $A_{18}{ }_{18}$ | IV |
| $296($ I) | 296 | $\boldsymbol{A}_{\mathbf{k}}^{8}$ | 306 | $\mathrm{A}_{2 \mu}{ }_{\text {\% }}$ |  |
| 296(I) | 290/288 | $2 B_{u}$ | 293 | $E_{u}{ }^{2}$ | - |
| $271(R)$ | 277/276 | $2 B_{8}$ | 281 | $E_{8}$ | VI |
| $255(R)$ | 266 | $\mathrm{A}_{8}{ }^{8}$ | 266 | ${ }_{18}^{8}$ | - |
|  | 200 | $B_{u}{ }^{\text {g }}$ | 202 | $B_{24}{ }_{8}$ | VIII |
|  | 202 | $\mathrm{A}_{8}$ | 198 | ${ }^{14}$ | - |
| 184(R) | 198 | $\mathrm{A}_{8}^{8}$ | 200 | $B_{18}{ }_{8}$ | VII |
| $165(\mathrm{I})$ | 175 | $B_{u}^{8}$ | 181 | $\mathrm{B}_{24}$ | x |
| 155(I) | 179/178 | ${ }^{2} B_{u}$ | 169 | $E_{u}$ | IX |

* Observed spectra from Clark \& Franks (1976).


V

$X$


Fig. 1. Thirteen molecular vibrational modes calculated for $\mathrm{Mo}_{2}\left(\mathrm{O}_{2} \mathrm{CCH}_{3}\right)_{4}$. The major axis of each ellipsoid indicates the magnitude and direction of the atom displacement and the arrows indicate the collective atom motion.

A comparison of our calculated vibrational energies and the observed IR and Raman bands for all compounds shows quite good agreement for both the isolated molecule and the crystal calculations. However, in some cases the specific assignments for the observed bands in the crystal are different from those for the molecule. In particular, the Raman modes at 277 and $253 \mathrm{~cm}^{-1}$ for $\mathrm{K}_{4} \mathrm{Mo}_{2} \mathrm{Cl}_{8} .2 \mathrm{H}_{2} \mathrm{O}$ are assigned to the molecular modes IV ( $A_{1 g}$ ) and


Fig. 2. Ten molecular vibrational modes calculated for $\mathrm{Mo}_{2} \mathrm{Cl}_{8}^{4-}$. The major axis of each ellipsoid indicates the magnitude and direction of the atom displacement and the arrows indicate the collective atom motion.

VI ( $E_{g}$ ), respectively, with very good agreement with the calculated values. In the crystal, however, the $\mathrm{Mo}_{2} \mathrm{Cl}_{8}^{4-}$ ion is strongly perturbed by two $\mathrm{K}^{+}$ions positioned on opposite sides of the $\mathrm{Mo}=\mathrm{Mo}$ bond. As a consequence the molecular $E_{g}$ mode is split into $B_{2 g}$ and $B_{3 g}$ modes with calculated values of 269 and $259 \mathrm{~cm}^{-1}$, respectively. Although the agreement is not as good as for the isolated-molecule calculation we prefer to assign both observed Raman modes to this split $E_{g}$ mode. Inclusion of interaction terms for $\mathrm{K}^{+}$ would probably increase the splitting and improve the match with the observed bands, but appropriate coefficients for $\mathrm{K}^{+}$are not available. Similarly the two IR bands at 182 and $160 \mathrm{~cm}^{-1}$ for this compound are assigned to the $B_{2 u}$ and $B_{3 u}$ modes arising from a split $E_{u}$ molecular mode (IX).

The poorest fit was obtained for [( $n$ $\left.\mathrm{Bu})_{4} \mathrm{~N}\right]_{2}\left[\mathrm{Re}_{2} \mathrm{Cl}_{8}\right]$ and is most apparent in the lowenergy region where the calculated vibrational energies are all higher than the observed values. This is probably due to our neglect of all the structural features and their appropriate interaction terms for the two ( $n-\mathrm{Bu})_{4} \mathrm{~N}^{+}$ions. This probably has an effect on our estimates of some of the force constants for this compound, but we expect that $K(R e R e)$ is unaffected because it only contributes to two higher energy modes, I and IV.

The most striking effect of our inclusion of more contributions to the force-field model is that our best values for the $M=M$ stretching force constants are considerably lower than those reported previously. For example, our value for $K(\mathrm{MoMo})$ is 1.7 $2.0 \mathrm{~N} \mathrm{~m}^{-1}$ as compared to a value of $3.8 \mathrm{~N} \mathrm{~m}^{-1}$ previously given for $\mathrm{Mo}_{2}\left(\mathrm{O}_{2} \mathrm{CCH}_{3}\right)_{4}$ by Bratton et al. (1971) and values of 3.5 and $4.5 \mathrm{~N} \mathrm{~m}^{-1}$ for $\left[\mathrm{Mo}_{2} \mathrm{Cl}_{8}\right]^{4-}$ and $\mathrm{Mo}_{2}\left(\mathrm{O}_{2} \mathrm{CCH}_{3}\right)_{4}$, respectively, reported by Ketteringham et al. (1976). Similarly our values for $K(\operatorname{ReRe})$ are markedly different from previously quoted values. Bratton et al. give $K(\operatorname{ReRe})$ values of $3.77 \mathrm{~N} \mathrm{~m}^{-1}$ for $\mathrm{Re}_{2} \mathrm{Cl}_{8}^{2-}$ and $4.47 \mathrm{~N} \mathrm{~m}^{-1}$ for $\mathrm{Re}_{2}\left(\mathrm{O}_{2} \mathrm{CCH}_{3}\right)_{4} \mathrm{Cl}_{2}$; while Ketteringham et al. report values of $\sim 4.5 \mathrm{~N} \mathrm{~m}^{-1}$ for both compounds. Our values are 1.9 and $1.0 \mathrm{~N} \mathrm{~m}^{-1}$, respectively, for these two compounds and indicate that the $\operatorname{Re}=\operatorname{Re}$ bond is considerably weaker in the latter molecule than in the former. Some support for this conclusion can be seen in an examination of the molecular-orbital diagrams for $M_{2} L_{8}$ and $M_{2} L_{8} X_{2}$ molecules (Cotton \& Wilkinson, 1980). In addition, our values of $K(M \equiv M)$ of $\sim 2.0 \mathrm{~N} \mathrm{~m}^{-1}$ are more in line with those for $K(M-M)$ and $K(M=M), 0.5$ and $1.0 \mathrm{~N} \mathrm{~m}^{-1}$, respectively (Shriver \& Cooper, 1980). Moreover, the $\mathrm{Re} \equiv \mathrm{Re}$ and $\mathrm{Mo} \equiv \mathrm{Mo}$ bonds in the two octachlorides probably have very similar strengths as would be expected from their bond order. As a test of our force-field model we substituted ${ }^{92} \mathrm{Mo}$ into our calculations for $\mathrm{Mo}_{2}\left(\mathrm{O}_{2} \mathrm{CCH}_{3}\right)_{4}$ and reproduced exactly the shift in the Mo $\equiv$ Mo stretch observed by Shriver,

Cooper, Hutchinson, Morgan \& Mathey (1979). Furthermore, if the value of $K(M M)$ is set to zero we see a drop of only $\sim 30 \%$ in the energy of the $M \equiv M$ stretch, indicating that most of the contribution to the force field at the metal atoms is from elsewhere in the structure. Clearly, the previous workers' neglect of the other contributions to the force field lead to a substantial overestimate of $K(M M)$ as well as an improper ranking of $K(M M)$ values for related compounds. Moreover, the use of a more generalized force field with fewer parameters has given us a vibrational model that is well determined by the available IR and Raman spectra without neglect of any interactions.

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## References

Bondi, A. (1964). J. Phys. Chem. 68, 441-451.
Bratton, W. K., Cotton, F. A., Debeau, M. \& Walton, R. A. (1971). J. Coord. Chem. 1, 121-131.

Brencic, J. V. \& Cotton, F. A. (1969). Inorg. Chem. 8, 7-10.
Busing, W. R. (1980). WMIN. Report ORNL-5747. Oak Ridge National Laboratory, Tennessee.
Clark, J. H. \& Franks, M. L. (1975). J. Am. Chem. Soc. 97, 2691-2697.
Clark, J. H. \& Franks, M. L. (1976). J. Am. Chem. Soc. 98, 2763-2767.
Costa, G., Pauluzzi, E. \& Puxeddu, A. (1957). Gazz. Chim. Ital. 81, 885-895.

Cotton, F. A. \& Brignole, A. B. (1972). Inorganic Synthesis, Vol. XIII, edited by F. A. Cotron, pp. 87-89. New York: McGraw-Hill.
Cotton, F. A., Frenz, B. A., Stults, B. R. \& Webb, T. R. (1976). J. Am. Chem. Soc. 98, 2768-2773.

Cotton, F. A., Mester, A. C. E. \& Webb, T. R. (1974). Acta Cryst. B30, 2768-2770.
Cotton, F. A. \& Wilkinson, G. (1980). Advanced Inorganic Chemistry, 4th ed., p. 1099. New York: Interscience.
Gilbert, T. L. (1968). J. Chem. Phys. 49, 2640-2641.
Johnson, C. K. (1976). ORTEPII. Report ORNL-5138. Oak Ridge National Laboratory, Tennessee.
Johnson, M. K., Cannon, R. D. \& Powell, D. B. (1981). Spectrochim. Acta Part A, 37, 995-1006.
Johnson, M. K., Cannon, R. D. \& Powell, D. B. (1982). Spectrochim. Acta Part A, 38, 307-315.
Ketteringham, A. P., Oldham, C. \& Peacock, C. P. (1976). J. Chem. Soc. Dalton Trans. pp. 1640-1642.

Kosmin, P. A., Surazhskaya, M. D., Larina, T. B., Kotelnikova, A. S. \& Misailova, T. V. (1980). Koord. Khim. 6, 1256-1258.
NaKamoto, K. (1963). Infrared Spectra of Inorganic and Coordination Compounds, p. 282. New York: John Wiley.
Pauling, L. (1960). The Nature of the Chemical Bond, 3rd ed., p. 261. Ithaca: Cornell Univ. Press.

San Filippo, J. \& Sniadoch, H. (1973). Inorg. Chem. 12, 23262333.

Schachtschneider, J. H. (1965). Normal Mode Programs. Technical Reports 57-65 and 231-264. Shell Development Co., Emeryville, California.
Shriver, D. F. \& Cooper, C. B. (1980). Advances in Infrared and Raman Spectroscopy, Vol. 6, edited by R. J. H. Clark \& R. E. Hester, pp. 127-157. Philadelphia: Heyden.

Shriver, D. F., Cooper, C. B., Hutchinson, B., Morgan, J. \& Mathey, Y. (1979). Inorg. Chem. 18, 2048-2049.

Shriver, D. F., Mathey, Y. \& Greig, D. R. (1982). Inorg. Chem. 21, 3409-3413.
Slater, J. C. (1964). J. Chem. Phvs. 41, 3199-3204.

# Relation Between Tetrahedron Connections and Composition for Structures with Tetrahedral Anion Complexes* 

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#### Abstract

For the classification of structures with tetrahedral anion complexes such as silicates or phosphates different parameters have been proposed, such as Zoltai's tetrahedral sharing coefficient or Liebau's connectedness and linkedness. Another parameter,

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labelled $T T$, is discussed here, which denotes the average per tetrahedron of the sum (over all four corners of a tetrahedron) of the number of tetrahedra which are connected with one corner of the tetrahedron considered. If there are only isolated or cornerconnected tetrahedra in the structure the $T T$ parameter corresponds simply to the average number of tetrahedron-tetrahedron connections per tetrahedron. The $T T$ parameter can be related to Zoltai's sharing coefficient and Liebau's connectedness and linkedness. The particular advantage of the introduction of the $T T$ parameter is that it can be obtained


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